Survey on Ant Colony Optimization

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Abstract—Although ant is not one of those smart creatures, when swarm, however co-operate with each other while forag-ing(in search of food) they have this great ability to unearth an optimal solution to their problem thus coming up with the shortest path from their nest to the food source in case of foraging. Ants grant excellent efficiency while solving combinatorial problems and also have the potential of combining with other algorithms with ease. This survey includes Generalized ant inspired algorithm and different applications of ant Colony Optimization (ACO).

Keywords—Ant Colony Optimization (ACO), Swarm intelligence, meta-heuristics, OpenCL

I. INTRODUCTION

With a rapidly growing world and technology there are many challenges to solve complex problems in an efficient way and in a quick time. Ant colony optimization is one of the optimization techniques that have the capability of combining with other algorithms and improving their efficiency. It gives even better results when it is parallelized as it is intrinsically parallel. ACO is one of the naturally inspired metaheuristic algorithms. ACO takes the inspiration from ants. In ACO, colony of ants moves from nest to food source through different paths initially. While moving they lay a special chemical substance called pheromone. This pheromone is used

for stigmergy (ant's interaction). Using this all ants select an optimal path from nest to food source after some time. This time period is the convergence time. Thus, ant colonies are capable of finding shortest path for their purpose which is the optimal solution. In fact, Ant colony optimization is a multi-agent system as here multiple colonies of ants are used to come across a solution for the given problem. The role of agents is depicted by artificial ants. These artificial ants explore for the solution space probabilistically to uncover different solutions and finally converge to find the optimal solution out of these candidate solutions. The motivation to ACO comes from swarm intelligence. In fact, ACO is a subset of swarm intelligence and is inherently a parallelizable technique [1]. In this survey, first we have generalized the ACO algorithm and then, we have explored few application areas in which initially we have explained the main concrete problem which have an exponential worst case complexity or have large applications but require more time.

II. BACKGROUND AND APPLICATIONS OF ACO

Ant colony optimization was proposed in early 90s. The first algorithm proposed was Ant system (AS) by Dorigo [4] [5] subsequent to which many variants were proposed. MAX-MIN ant system and AS_{rank} are among the efficient algorithms of ACO. All the

variants use a general concept in which stochastic state transition rules which are function of pheromone value and heuristic information and two other parameters and are used and are used to control the effects of pheromone and heuristic information so that in different scenarios we can adjust these two values accordingly and obtain the desired optimal result. Here we use α and β are adjustable parameters to adjust relative influence of probability and heuristic information.

$$P^k = (\tau, \eta, \alpha, \beta)$$

where, P^k_{ij} = Probability with which ant k moves from i node to j.

η = heuristic information.

τ = pheromone trail update.

Local pheromone updates are done by the ant after local solution construction. After the evaluation of all local solutions global pheromone update is performed thereafter. The two main phases of ACO are- solution construction and pheromone update. During Solution construction decisions are undergone on the basis of above probabilistic rule and on discovery and evaluation of local optimal solutions; global pheromone update is carried out. Initialize Rules are used in different ACO algorithms like AS, AS_{rank}, Max-Min AS, ACS.

```
1   Loop
2       {
3           Loop
4               {
5               Ants or colony of ants will apply state
                transition rules and local pheromone update.
6               }
7
8           Until each finds a local solution
9           }
10      Global pheromone update after solution evaluation
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This choice depends on the type of problem we encountered with. There exists a diverse problem range that acquires bulk of time accompanied with a large search space. Consequently, their performance can be enhanced by using some Meta heuristic algorithms in an attempt to shrink the search space. Some of the Meta heuristic algorithms are particle swarm optimization, ant colony optimization and genetic algorithm. ACO unearth a large number of applications, especially problems which are NP-Hard. As NP-Hard problems have an exponential worst case complexity [6], so ACO can be pooled with them to trim down the complexity to polynomial time which can further be improved if it is parallelized. There are an assortment of areas where ACO algorithms are applied like in routing, assignment problems, scheduling problems [7], data mining and classification [8], emergency path rescue [9] and wireless sensor networks [10]. This survey will be confined to only a handful of these problems therefore restricting our discussion to those.

2.1 ACO APPLICATIONS IN ROUTING PROBLEMS

Concrete Problem: In routing there are various applications like sequential ordering, vehicle routing and others. Vehicle routing problem (VRP) [4] is actually a distribution management problem in which we need to serve n customers located at some given distance from a central depot. We are provided with a fleet of vehicles, customer's demand and travel time between two customers. The requirement is to minimize the travel time starting and ending at depot and each customer should be visited exactly once. Vehicle routing problem with time limitations is referred as VRPTW [4] vehicle routing problem with time window constraints. Our goal is to minimize number of vehicles used to minimize total

travel time [4] along with the constraint to visit each customer only once. ANT inspired approach: Till date the most successful ACO algorithm applied on VRPTW is multiple ant colony system (MACS). In MACS-VPRTW multiple colonies of ants are used to attain each of the above specified goals. The core idea is to reduce the convergence time, that why both colonies are implemented parallel. The constructed graph consists of the node representing customer locations and central depot which we call the source. Weights assigned to the edges connecting the nodes are the measure of distance between them and the pheromone trails (I, j) associated with each edge are the measure of desirability of visiting customer j after i. Initially, these weights are assigned a constant value of (i, j). Then each ant uses a probabilistic rule to take decisions and update the pheromone on the edges. Both the colonies of ants having different objectives use different set of pheromones. When both the colonies converge to local solutions satisfying the above two constraints, evaluation is done and final global optimal solution is established. ACO is accompanied by some local search procedure like simulated annealing and 2-optimal local search. In local search generally some permutations or exchanges are performed in the local solution aimed to uncover closer optimal solutions in a quicker time.

2.2 ACO applications in scheduling problems

Concrete Problem: Scheduling problems in a generalized way deals with assigning available resources to tasks. There a number of ACO algorithms proposed for scheduling problems ranging from job shop problem (JSP) and open shop problem (OSP) to permutation flow shop problem (PFSP). In flow shop scheduling (FSP) [7] problem independent jobs and machines are given and these jobs are to be assigned to machines. Every job has some operations and these operations are to be processed on one of the machines available in a non-preemptive fashion. Our goal is to assign all these jobs to machines in such a way, that all the operations are processed in a minimum time period. The total completion time thus obtained should be minimizing. In this scenario, initially a different order of job execution on machines will be generated followed by preparation of Gantt chart depicting the completion time of jobs. The order which offers minimum completion time span in the Gantt chart acts as our solution. Ant inspired approach: here will be a number of permutations to this assignment problem, so ACO is applied to this problem in which each ant generates a solution concurrently and among these solutions best one is selected and global pheromone update rule is applied. Therefore, using probabilistic-tic rules and pheromone update rule we manage to drop off our search space and eventually the number of permutations and ACO leads to comparatively faster solution detection. In this problem, we can use the standard and earliest form of ACO which is Ant system [4]. So state transition and update rules of Ant system will be applied and a table Job/order will be maintained having each cell representing pheromone value associated with assigning job a particular order. Here also some local search procedure will be used in which some jobs will be interchanged to come up with closer optimal solutions.

2.3 ACO applications for Ad hoc networks

Concrete Problem: In mobile ad hoc network

(MANET) [1] there is no fixed network topology as all the nodes are mobile which described the reason they are referred as infrastructure less networks. In ad hoc networks routing approaches consists of table driven approaches and on demand approaches. We will be using on demand routing here. One algorithm named Ant colony based routing algorithm (ARA) has already been implemented for ad hoc networks in [1]. Our goal is to trace the shortest path between each pair of nodes that is APSP for MANET. ANT inspired approach: Here every node will maintain a routing table having all the nodes in the network and pheromone value indicating the preference with which this node can be selected from the neighboring nodes. Ant keeps the track of all the visited nodes and maintains a stack of these nodes. This offers convenient selection of the highest probability node from the unvisited nodes which may lead to the best path.

III. ANT Colony Optimization Algorithm

Ant colony optimization [1] [2] [6] was proposed in early 90's. The first algorithm proposed was Ant system (AS) by Dorigo subsequent to which many variants were proposed. Among all of them Max-Min Ant system provides best results in most of the cases. All the variants use a general concept in which stochastic state transition rules which are function of pheromone value and heuristic information and two other parameters α and β are used to control the effects of pheromone and heuristic information so that in different scenarios we can adjust these two values accordingly and obtain the desired optimal result. There are two main phases of every Ant inspired algorithm. These are:-

❖ Solution construction
❖ Pheromone update

a) Solution construction: Ant select next node to be cited using a stochastic rule. Ant 'k' at node 'i' has the following probability to select node j as next node at time 't'

$$p_{i,j}^k = \frac{[\tau_{i,j}]^\alpha [\eta_{i,j}]^\beta}{\sum_{l \in N_i^k} [\tau_{i,l}]^\alpha [\eta_{i,l}]^\beta}, \qquad if \; j \in N_i^k$$

Where, p_{ij}^k = Probability with which ant k moves from i node to j.

η_{ij} = heuristic information.

$\tau_{ij}(t)$ = pheromone trail update.

And this heuristic information depends on the edge length. Parameters α and β are adjustable to relative influence of probability and heuristic information.

b)   Pheromone update: After all ants have constructed their tours pheromone trails are updated. This is done by first lowering the pheromone value on all edges by a constant factor called evaporation rate:

$$\tau_{ij} \leftarrow (1-\rho) \cdot \tau_{ij}, \text{ for all } (i,j) \in L$$

After evaporation all ants deposits pheromones on the edges they have visited in their tours.

$$\tau_{ij} \leftarrow \tau_{ij} + \sum_{k=1}^m \Delta \tau_{ij}^k, \text{ for all } (i,j) \in L$$

Where,

$$\Delta \tau_{ij}^k = \begin{cases} 1/C_k, & if \; (i,j) \in T_k(t) \\ 0, & otherwise \end{cases}$$

Where C_k is the length of the tour T^k built by ant k having the best optimal solution.

In Ant System the above process which comprises of solution construction and pheromone update is for a colony of ants. If there is more than one colony of ants then both the colonies will have one local pheromone update matrix and will share one global pheromone update matrix.

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